



27/07/2015

## Monte Carlo Validation

Application for RIO interpolation model

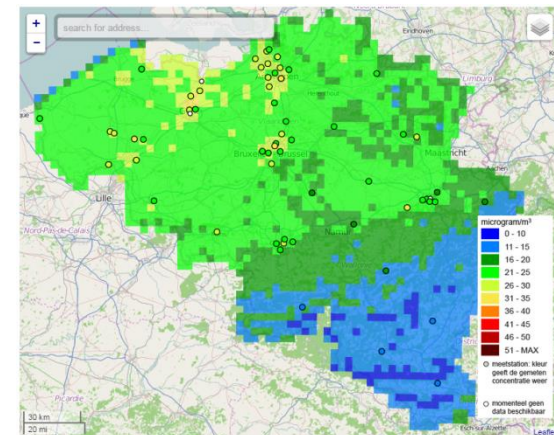
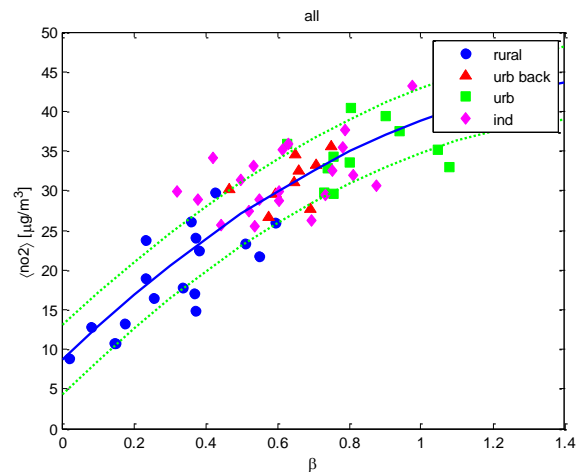
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# Outline

- » RIO in 1 slide
- » RIO validation, what is “the model” ?
- » Monte Carlo validation
  - » Some analyses
  - » Impact on target plot results for RIO
- » Conclusions

# The RIO model in 1 slide

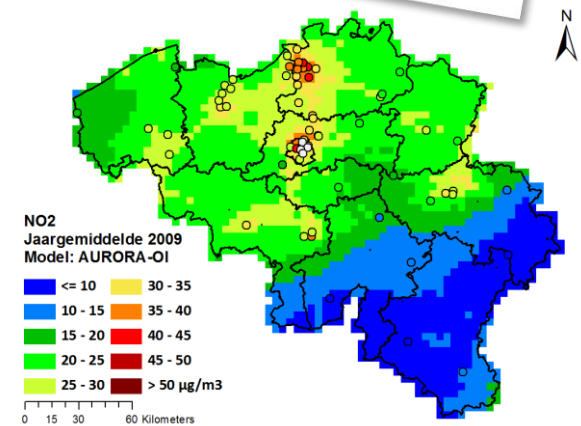
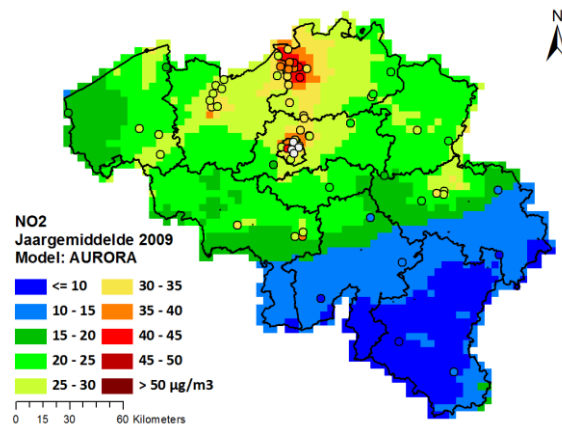
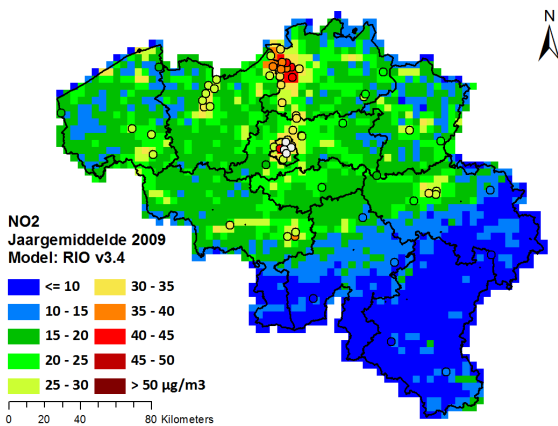
- » Detrended Kriging interpolation model
- » Spatial trend captured by trendfunctions expressed vs. land use regression parameter  $\beta$  (CORINE).
  - » per hour of the day, week/weekend



- » Operational mapping model in Belgium (IRCELINE) & Netherlands (RIVM)

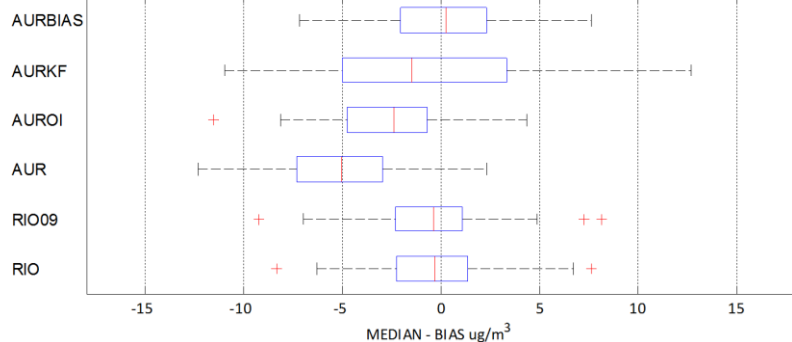
# RIO validation

- » Elaborate model comparison (2012)
  - » RIO (Interpolation model)
  - » AURORA CTM ( + calibration/DA: OI)
  - » OPS
- » 2009, Traffic stations
- » Leaving one out

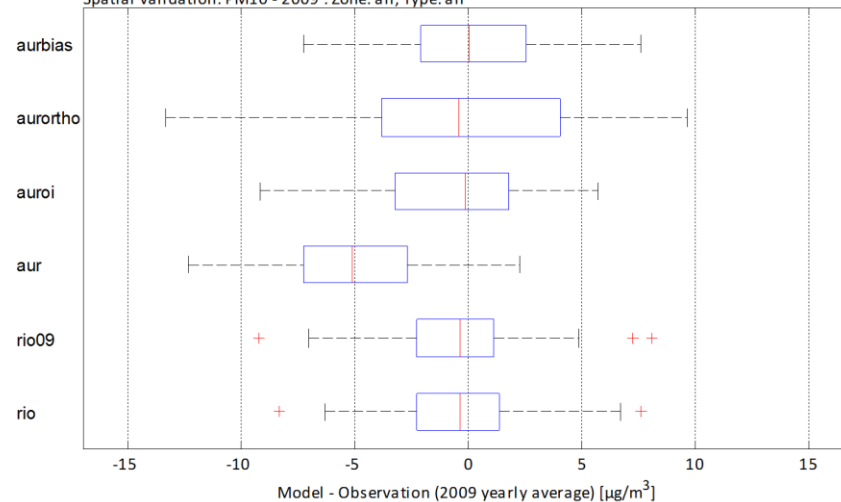


# Model comparison exercise

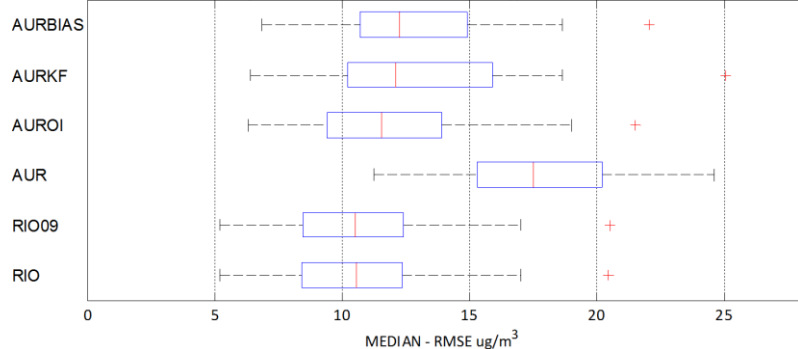
Time-series validation per station: PM10 - 2009 : Zone: all, Type: all



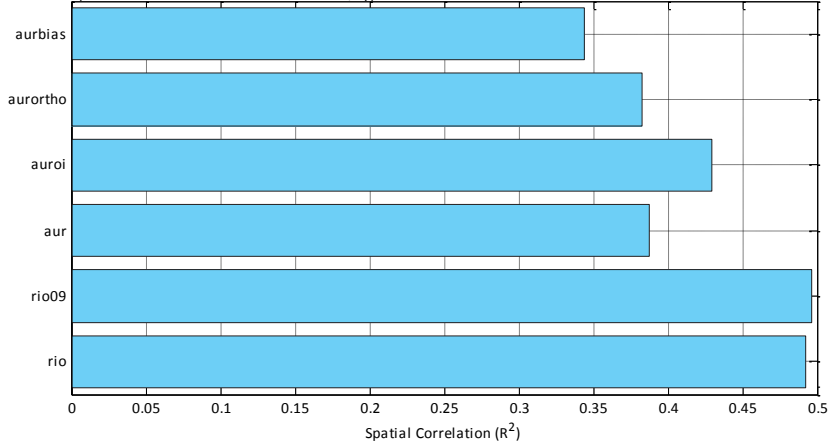
Spatial validation: PM10 - 2009 : Zone: all, Type: all



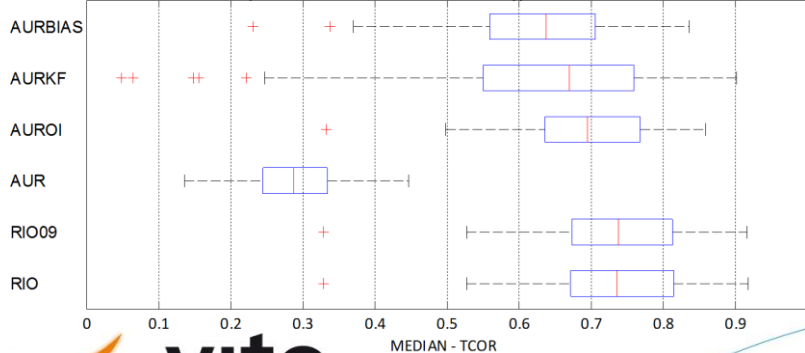
Time-series validation per station: PM10 - 2009 : Zone: all, Type: all



Spatial validation: PM10 - 2009 : Zone: all, Type: all

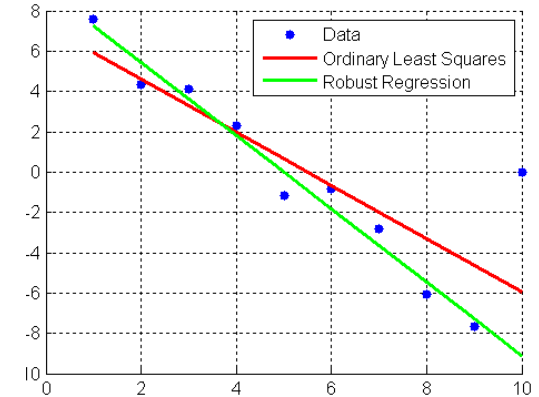
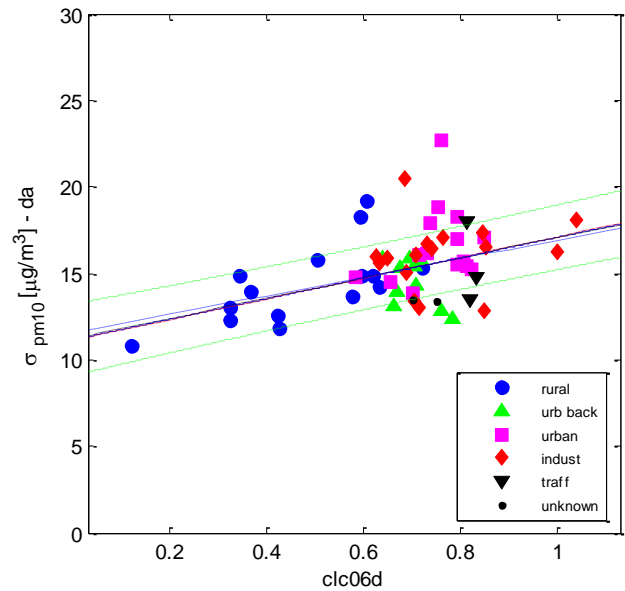
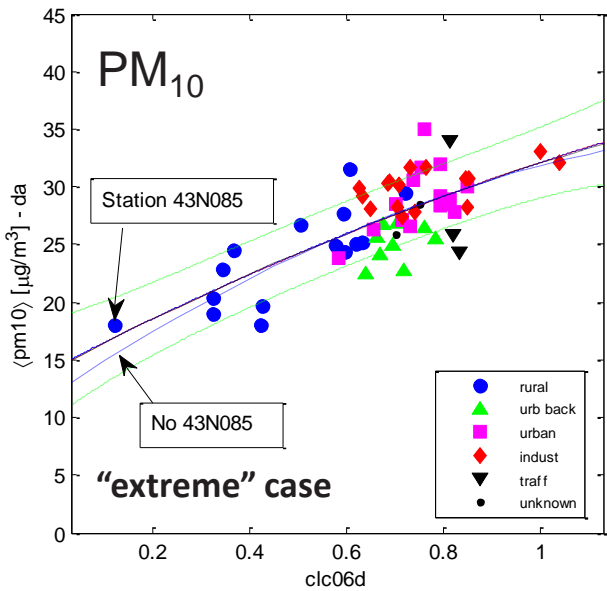


Time-series validation per station: PM10 - 2009 : Zone: all, Type: all



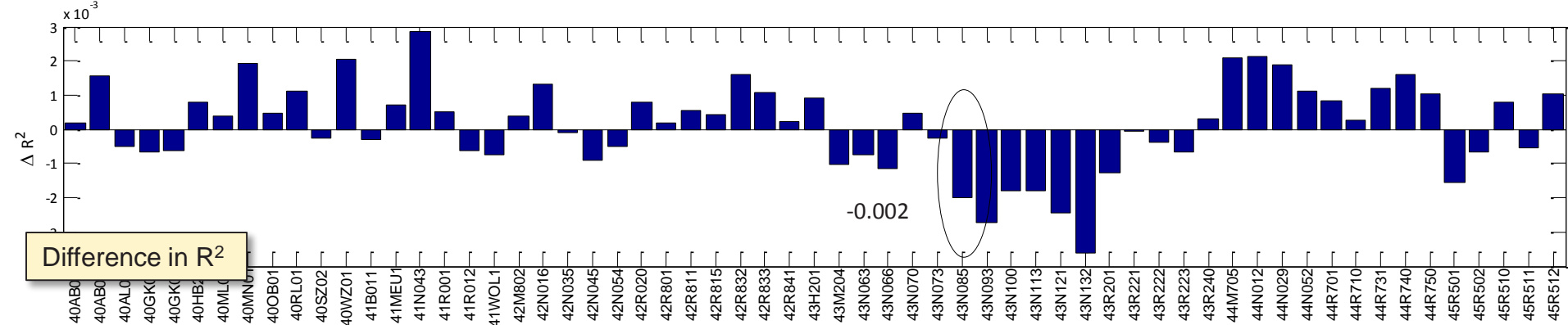
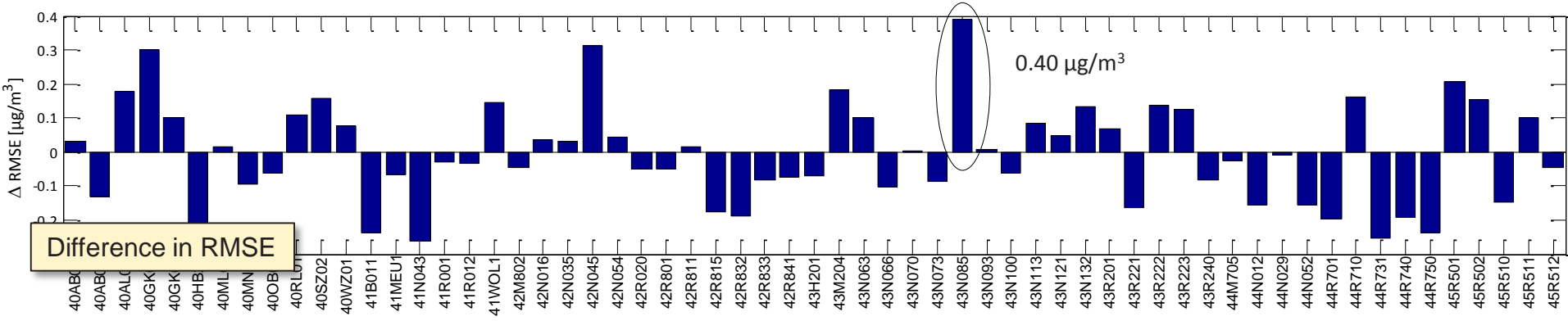
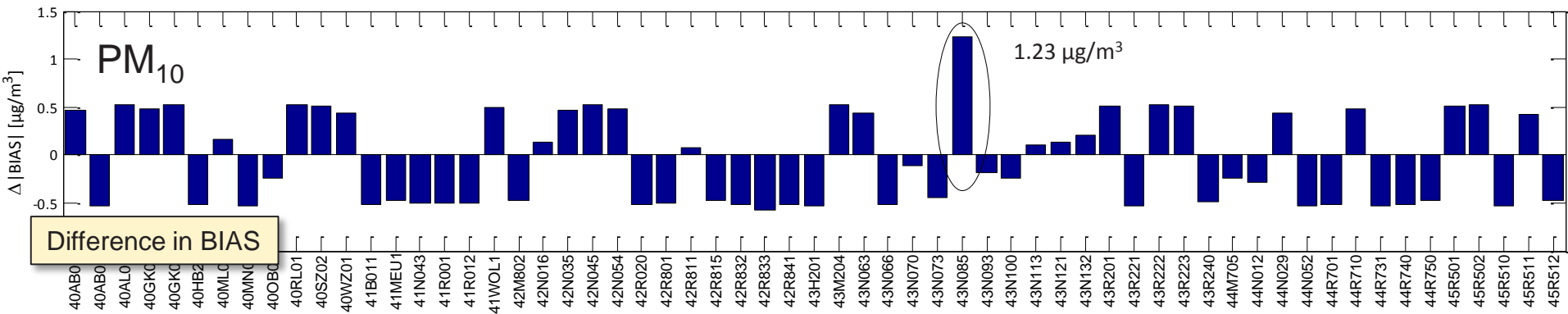
# DA/interpolation model-calibration ?

- » RIO uses measurements
  - » Model configuration : trendfunctions, long term averages, spatial correlations, land use regression weights ( $\beta$ )
  - » Interpolations : hourly measurements from available stations
- » DA (e.g. OI) similar !
  - » Model configuration : error covariance matrices...
- » Leaving-one-out : what do we leave out ?
  - » → RIO : influence of leaving out one station in trend fitting



# Impact on (temporal) validation statistics

Vershil in validatie statistieken: Geen 43N085 t.o.v. basis RIO v3.4



# Some thoughts

- » Differences relatively small compared to differences in RMSE, BIAS &  $R^2$  between models
- » How do we define the “model” in this case ?
  - » Trendfunctions, spatial correlations, long term averages considered part of the model.



# Monte Carlo validation

- » MC methodology (C. Carnevale)
- » **repeat until** (each station is left out at least once ( $=n_{\min}$ )):
  - » leave N stations out at random (typ. 20 %)
  - » validate
  - » compute RMSE for stations that were left out
- » Use validation statistics of series which give worst RMSE in  $\Delta$ -tool

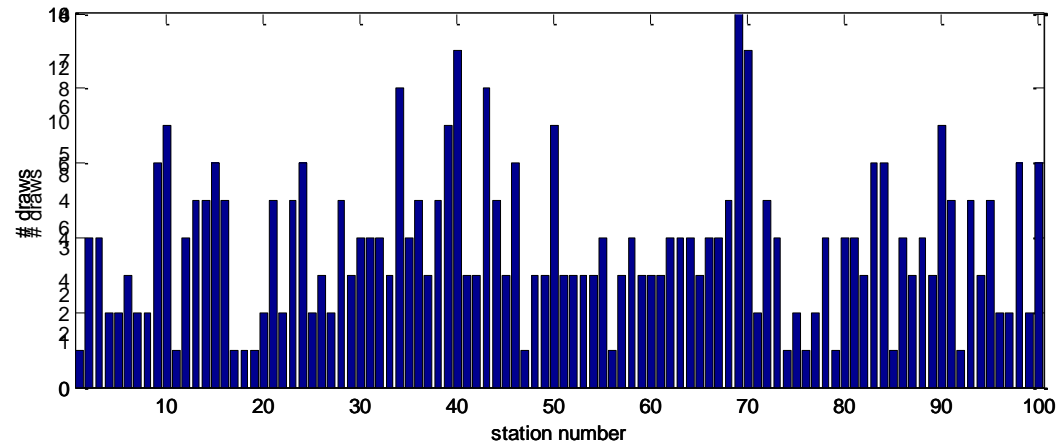
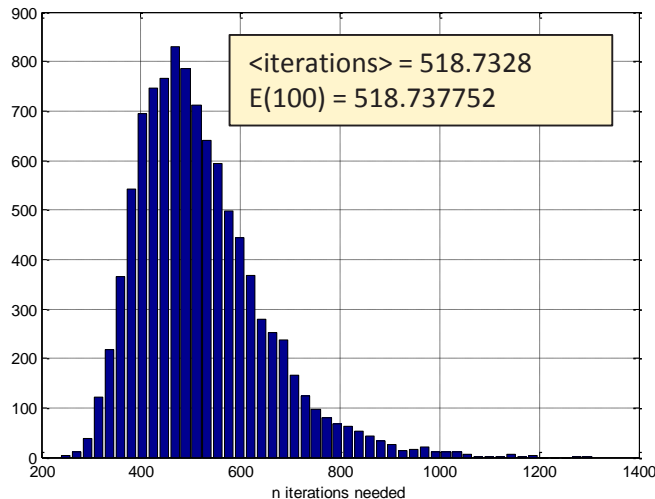
# “Coupon collector’s problem”

- » “Given  $n$  coupons, how many coupons  $X$  do you expect you need to draw with replacement before having drawn each coupon at least once?”

- » [https://en.wikipedia.org/wiki/Coupon\\_collector%27s\\_problem](https://en.wikipedia.org/wiki/Coupon_collector%27s_problem)

- » 
$$E(X) = n \sum_{i=1}^n \frac{1}{i}$$

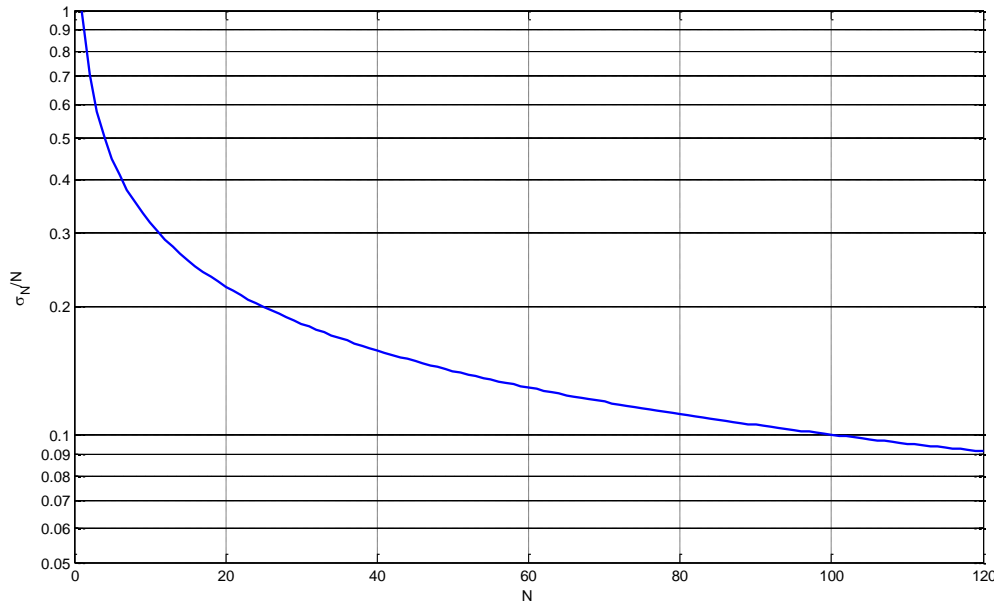
$N=100, m=1, n_{\min}=1$



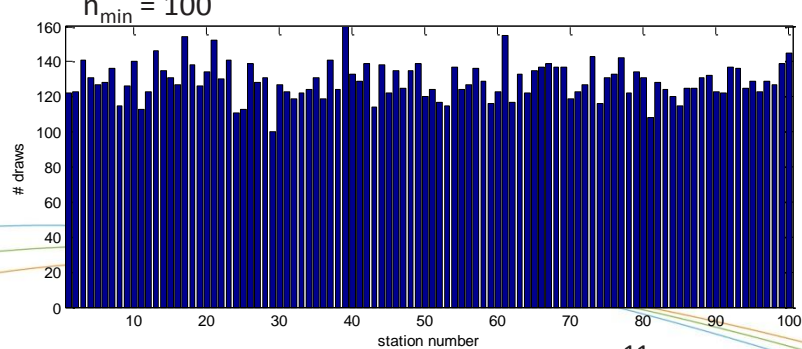
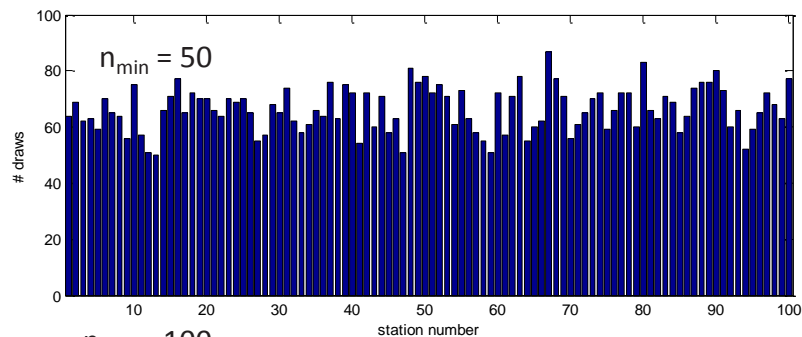
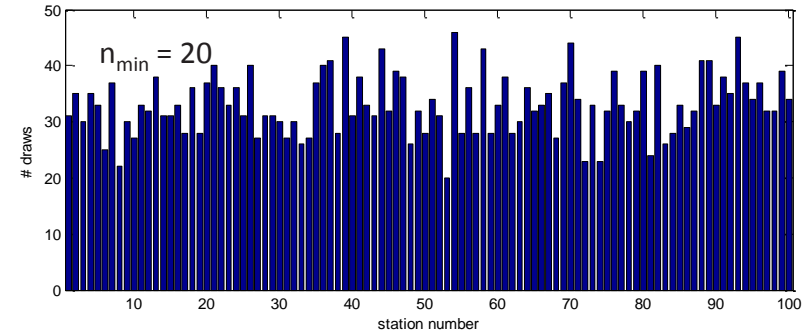
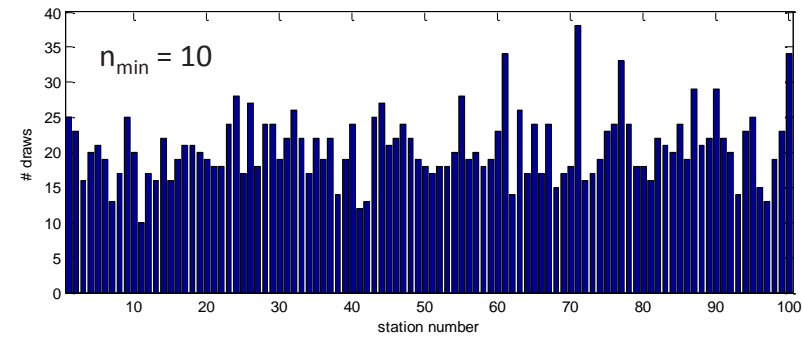
- » Depending on chance some stations are selected 1 times, some  $> 10$  times

# Monte Carlo validation

- » Select each station at least  $n_{\min}$  times
- » How many times a station is drawn

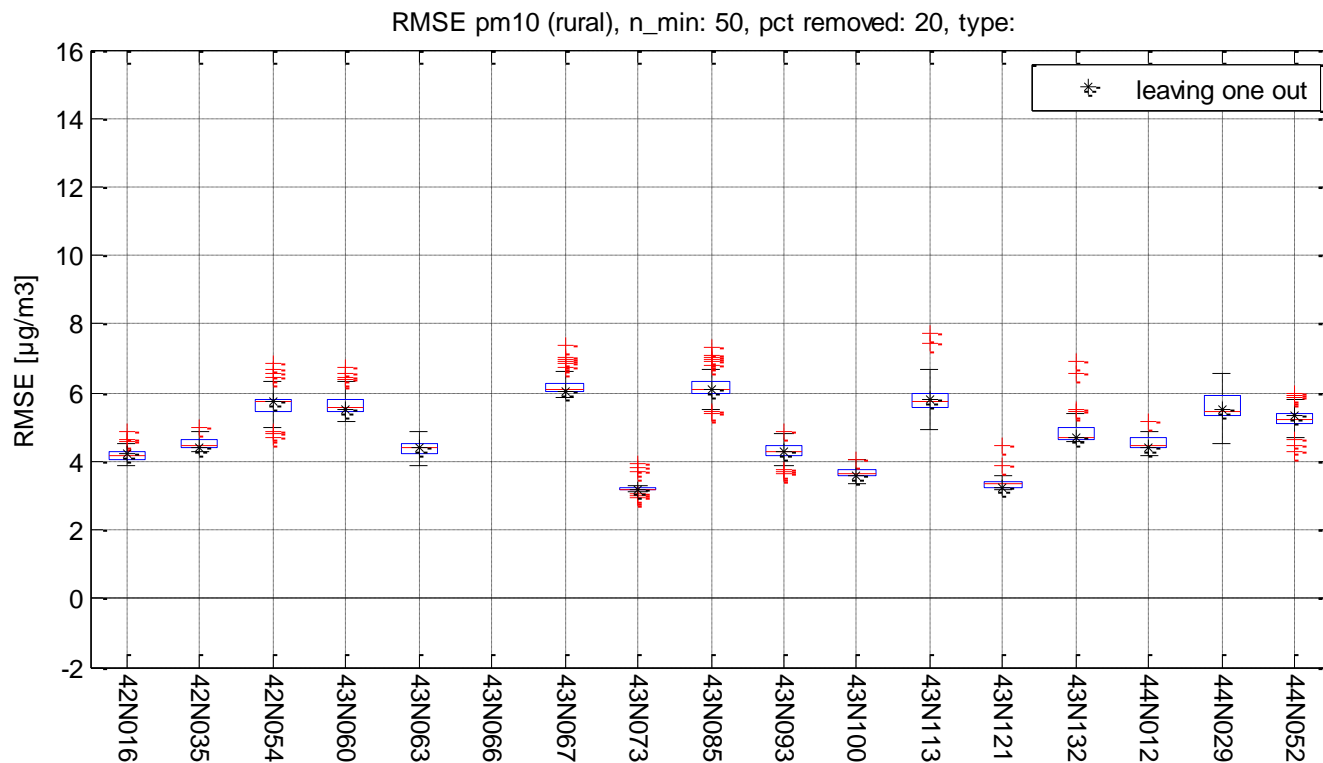


- » How robust is the validation ?



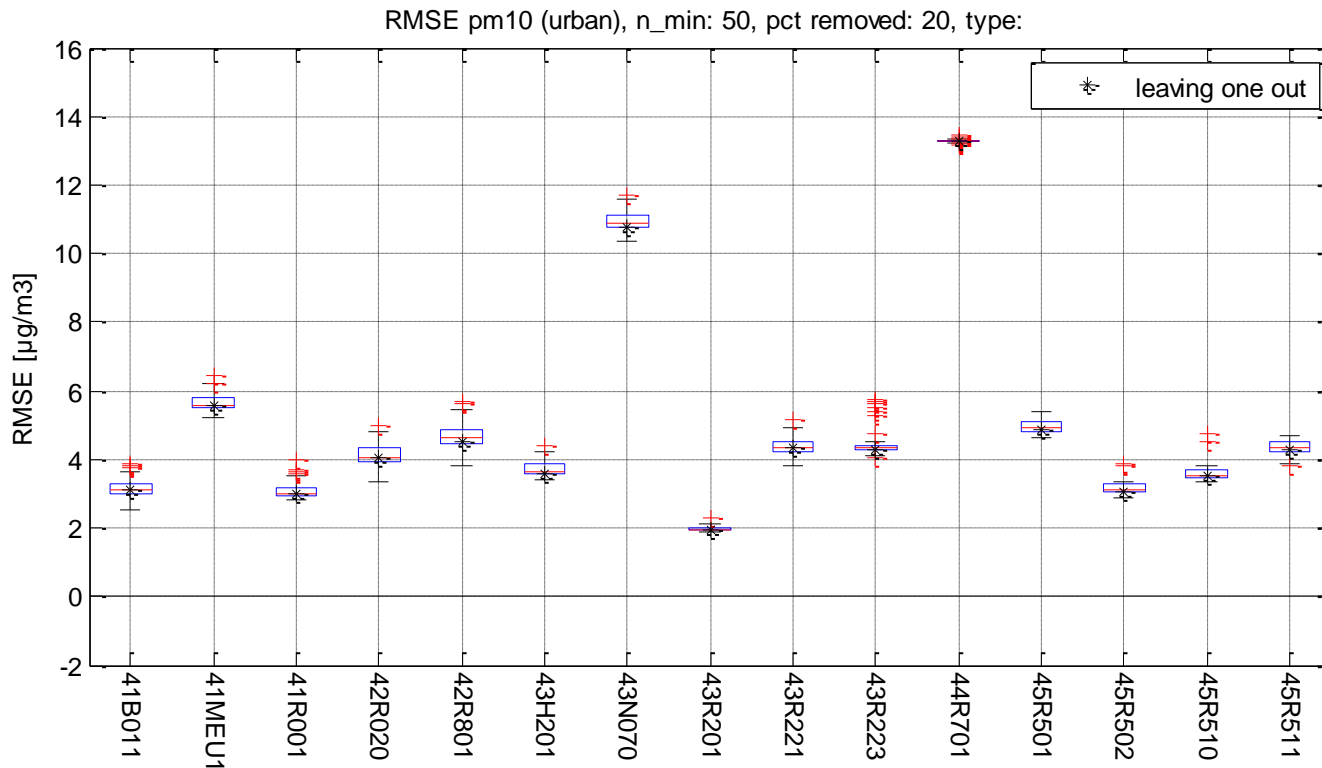
# RIO Monte Carlo Validation

## RMSE – rural vs. n\_min



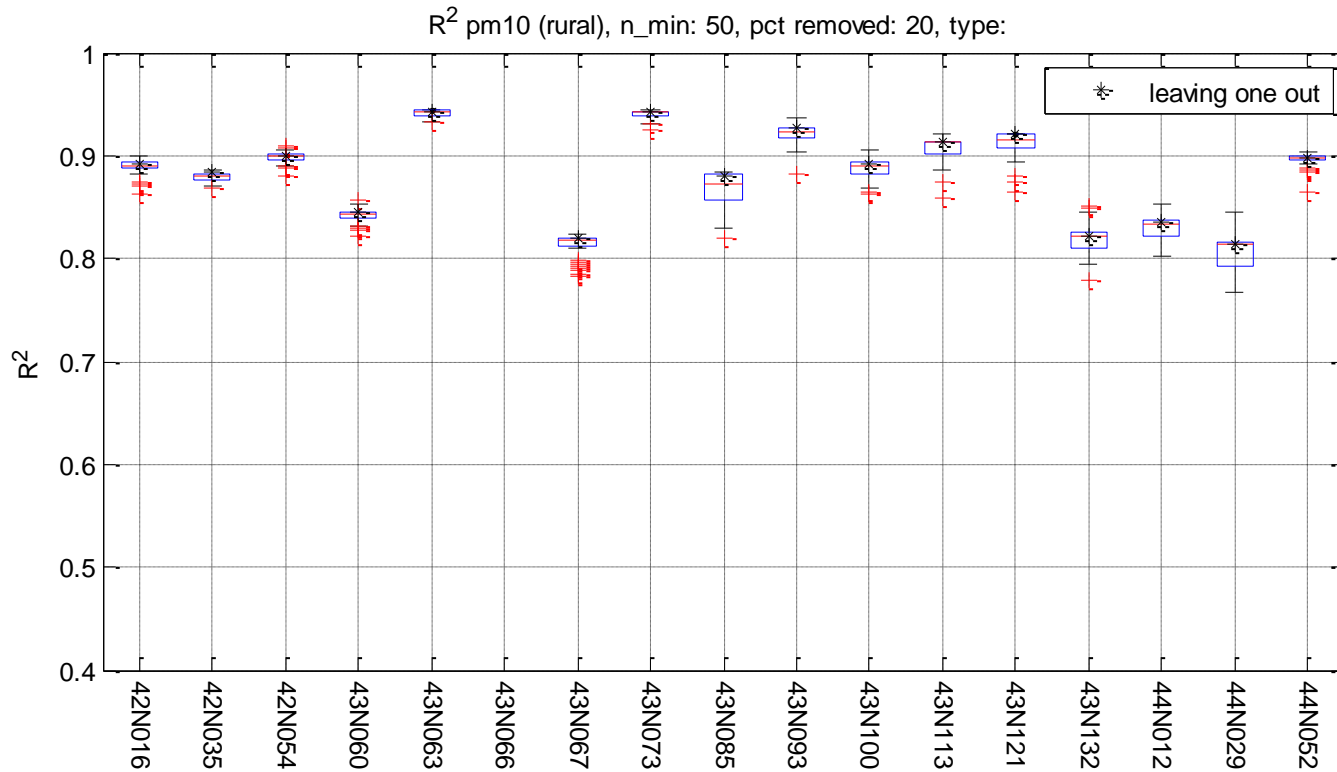
# RIO Monte Carlo Validation

## RMSE – urban vs. n\_min



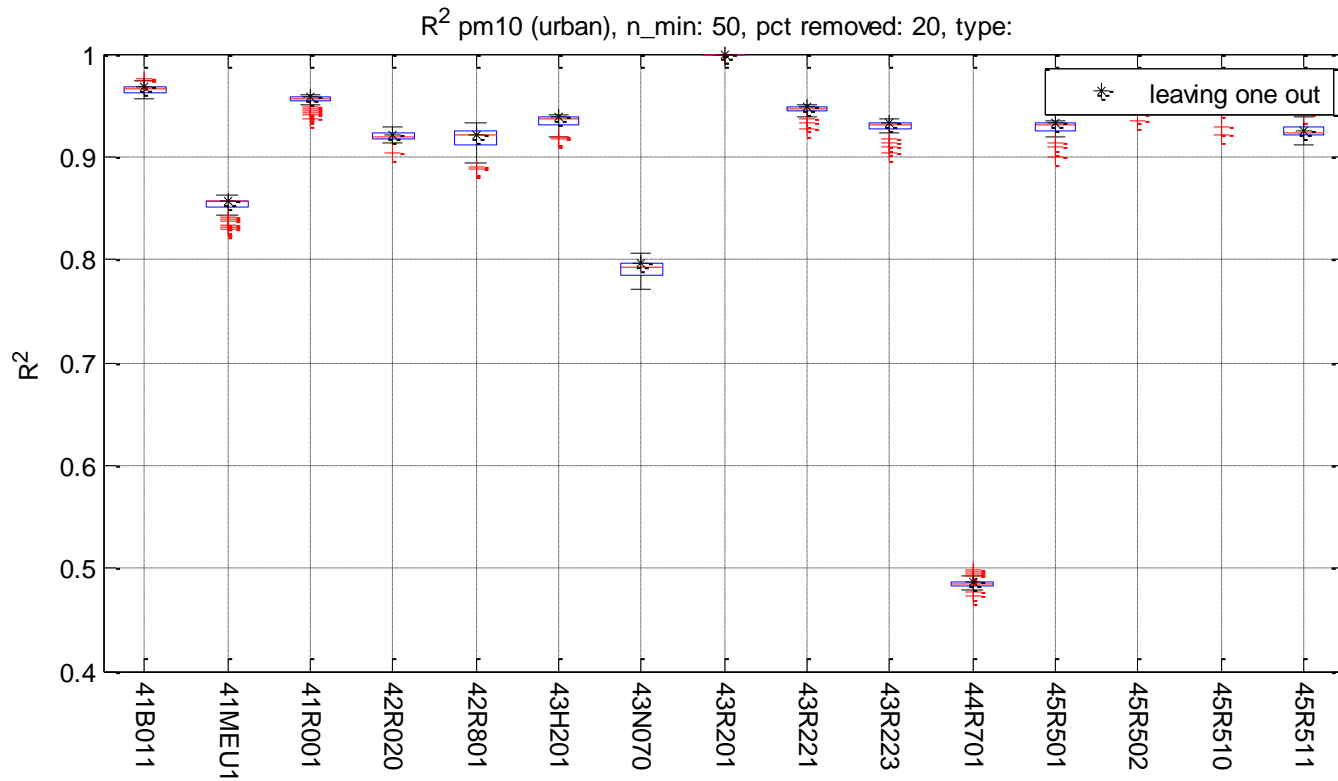
# RIO Monte Carlo Validation

## R2 – rural vs. n\_min



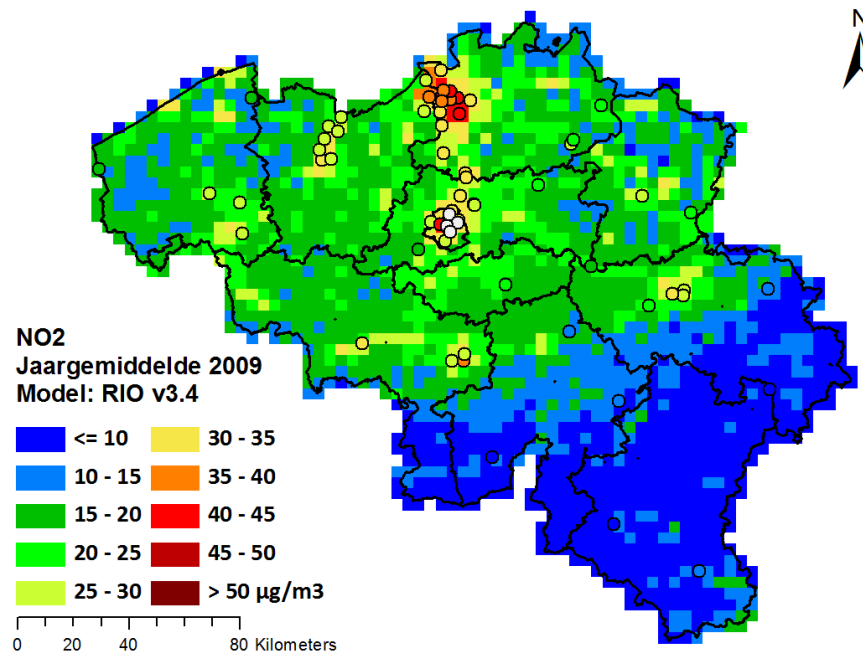
# RIO Monte Carlo Validation

## R2 – urban vs. n\_min



# Observations

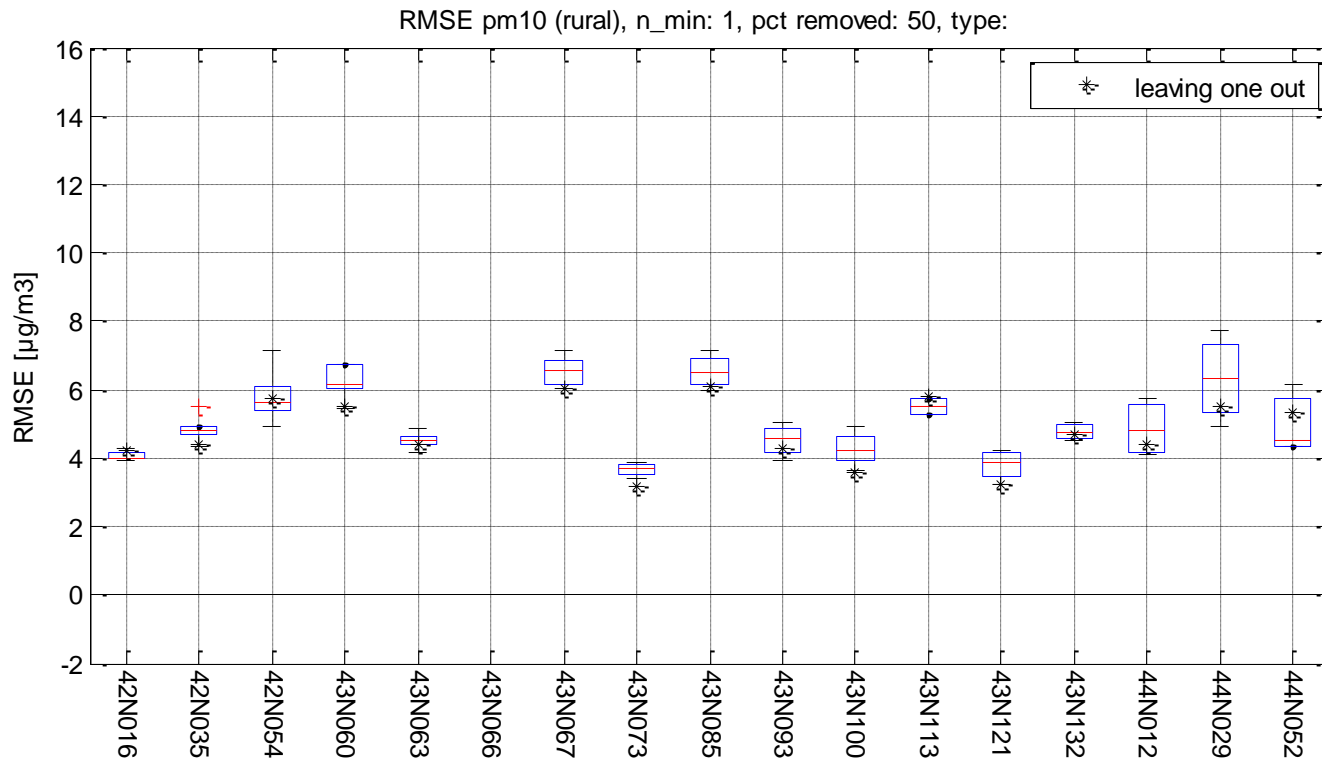
- » No dramatic differences w.r.t. the percentage of stations removed
- » Leaving one out does not necessarily yield best RMSE !
- » Clustering of stations





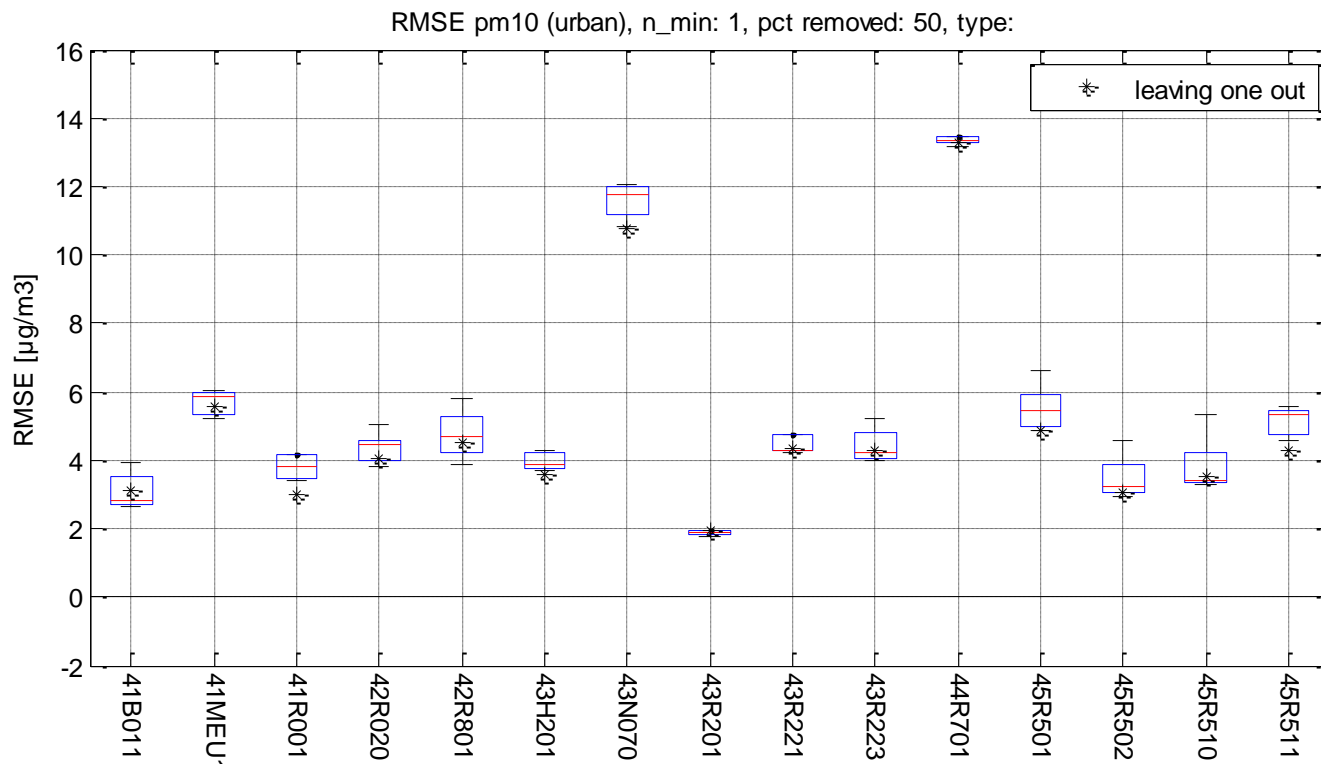
# RIO Monte Carlo Validation

## PM10 - rural vs. pct. removed



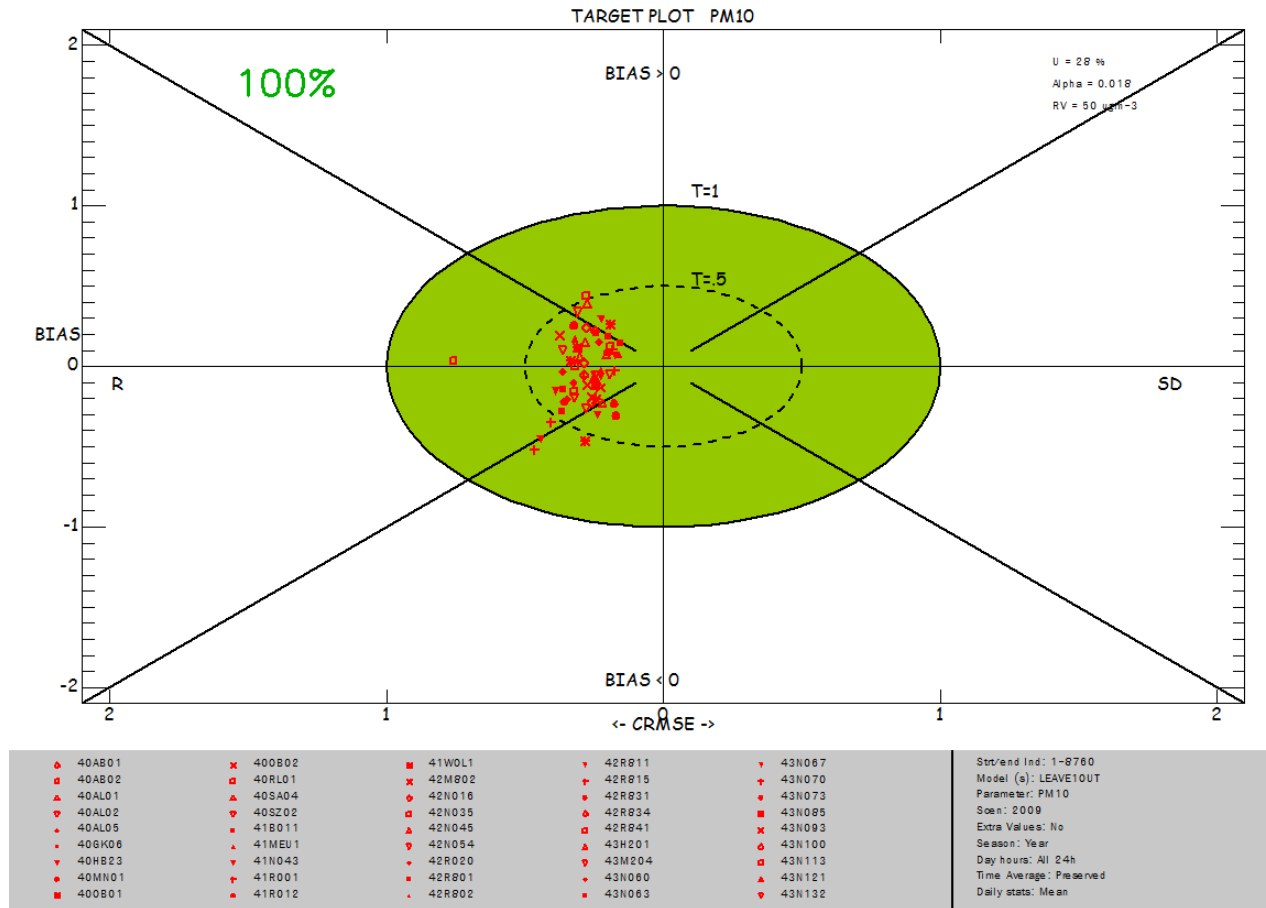
# RIO Monte Carlo Validation

## PM10 – urban vs. percentage removed



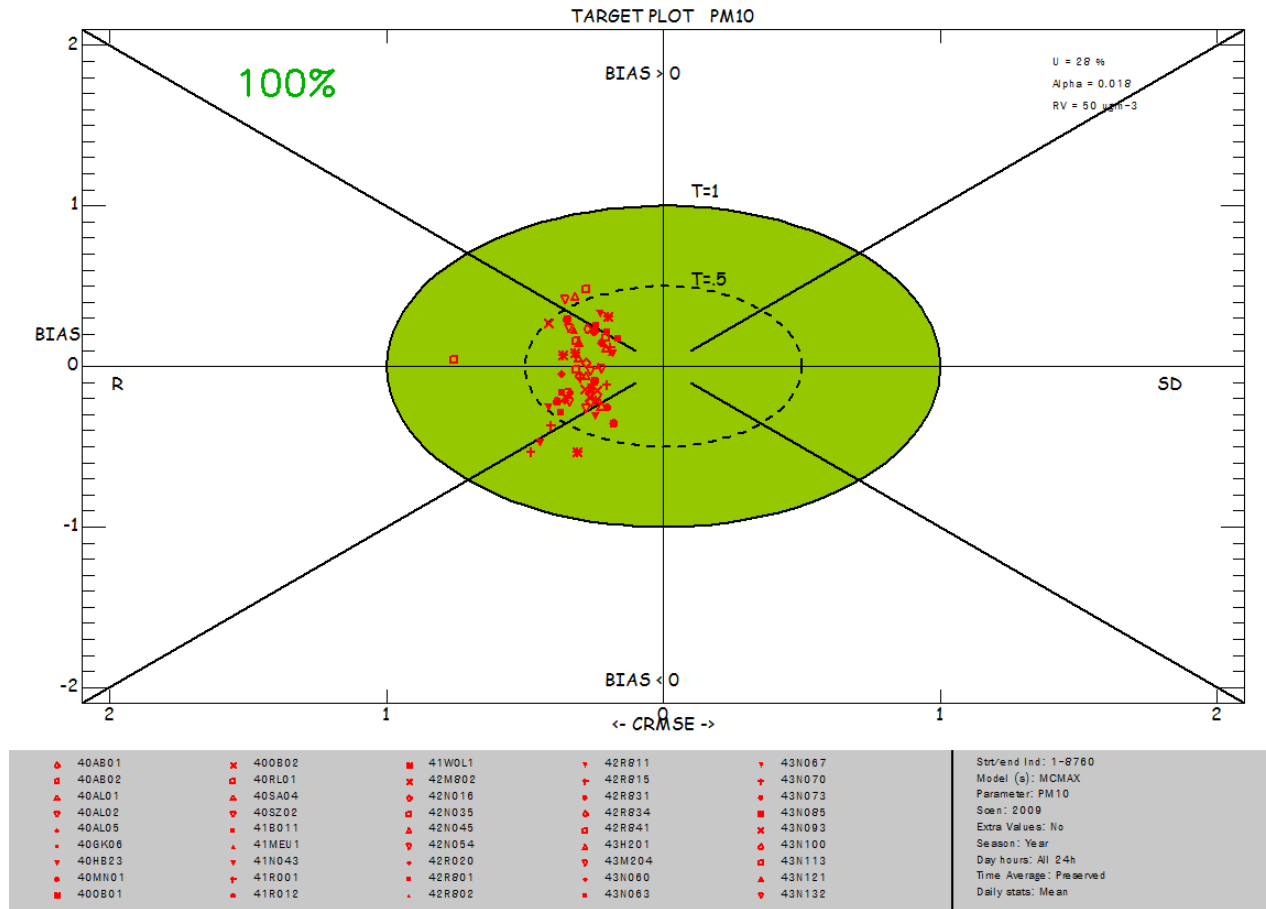
# Validation in $\Delta$ tool

- » PM10 da 2009
- » Leave 1 out



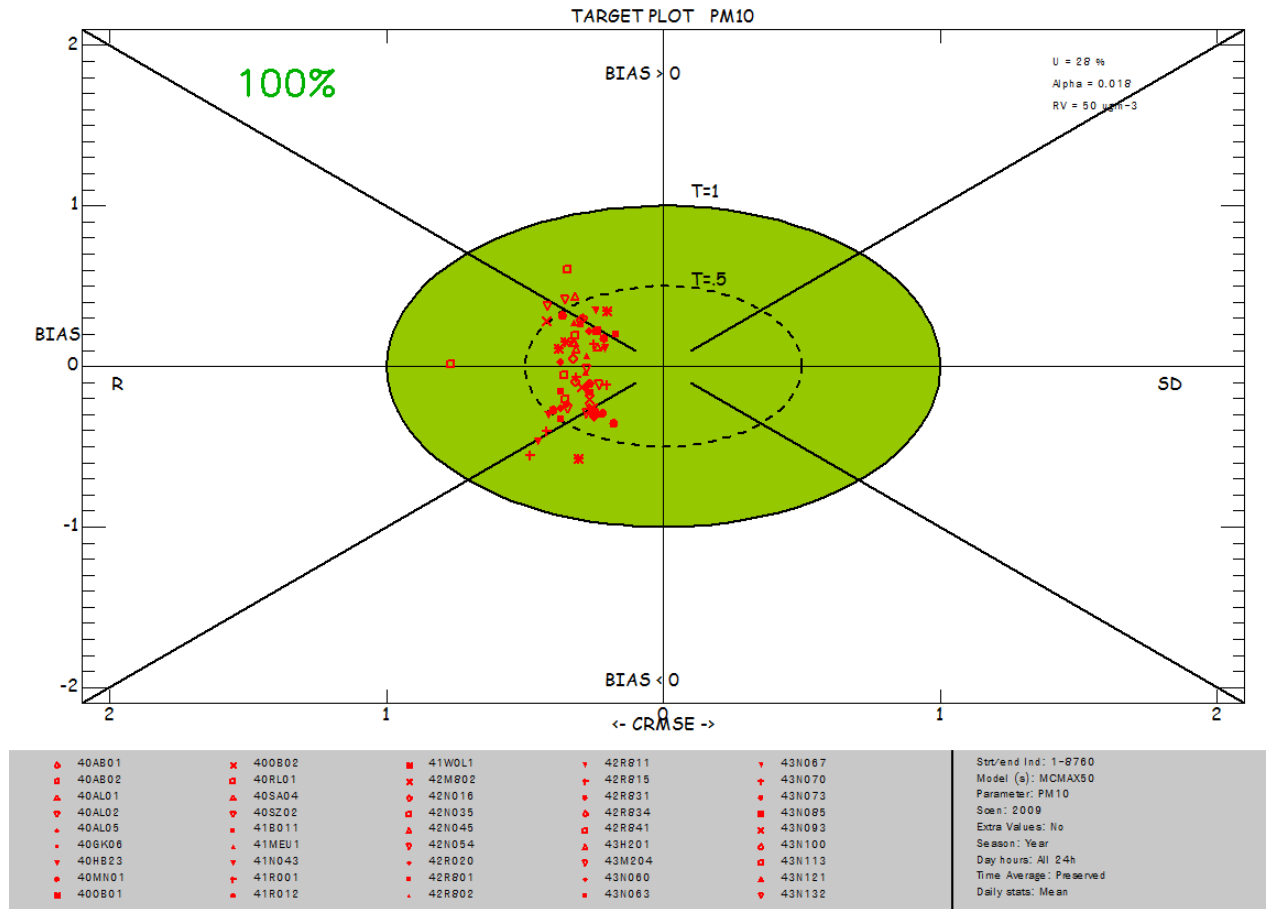
# Validation in $\Delta$ tool

- » MC Validation
- »  $N_{\min} 1$
- » Worst RMSE



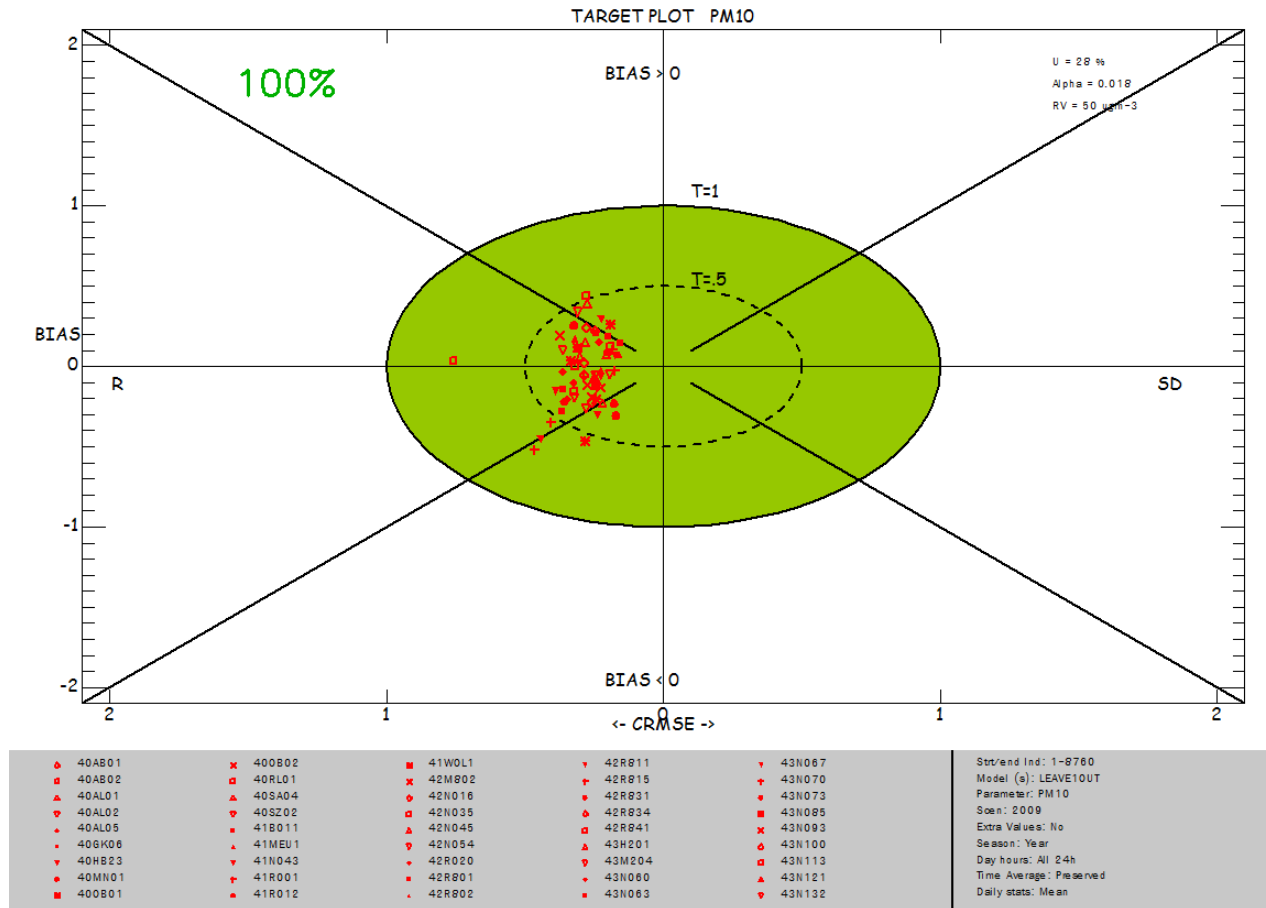
# Validation in $\Delta$ tool

- » MC Validation
- »  $N_{\min}$  50
- » Worst RMSE



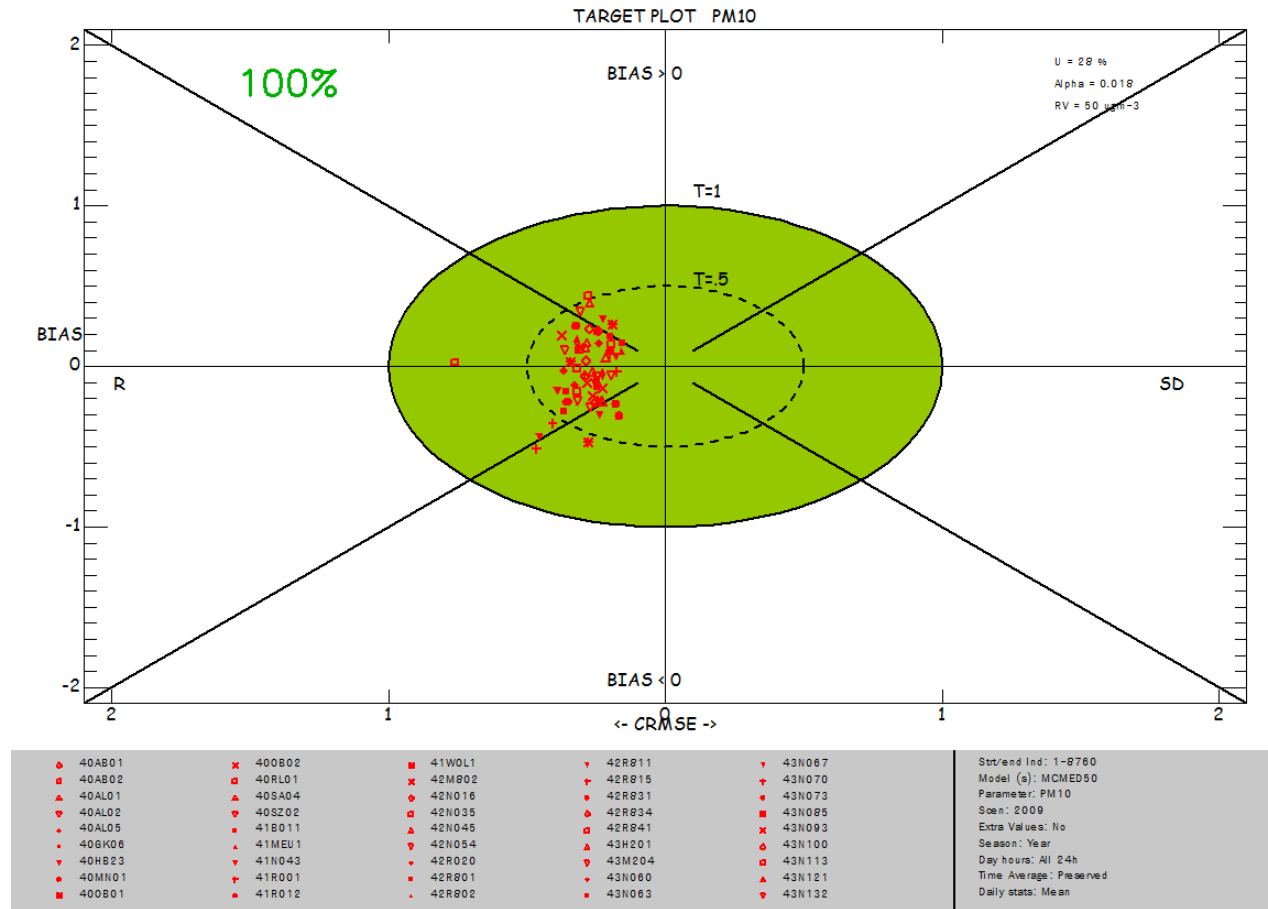
# Validation in $\Delta$ tool

- » PM10 da 2009
- » Leave 1 out



# Validation in $\Delta$ tool

- » MC Validation
- »  $N_{\min}$  50
- » Median RMSE



# Conclusions & discussion

- » What is “the model” ?
- » Monte Carlo method seems to be quite robust for RIO w.r.t. leaving-one-out (at least for  $PM_{10}$ )... at first sight.
  - » Clustering of stations in urban area's
  - »  $PM_{10}$  more regional pollutant → rural stations
- » Look at other pollutants ( $NO_2$ ,  $O_3$ ) to confirm/reject
- » Monte Carlo method not always yield worse statistics when looking at median
- » Using worst RMSE is sensitive to  $N_{\min}$ 
  - » Need to check what is happening with the distributions : increase in outliers
- » At the moment : using daily averages
  - » Computation time could become issue (for a “simple validation”)